

Exercise 4.1a

Wavelength & Frequency

Name: _____

Date: _____ Per: _____

The Planck constant (denoted h), also called Planck's constant, is a physical constant used to describe the sizes of quanta in quantum mechanics. It is named after Max Planck, one of the founders of quantum theory. The Planck constant is the proportionality constant between energy (E) of a photon and the frequency of its associated electromagnetic wave (ν). This relation between the energy and frequency is called the Planck relation or the Planck–Einstein equation:

$$E = h\nu$$

Using the following simple relation between frequency (ν), speed of light (c), and wavelength (λ),

$$\nu = \frac{c}{\lambda}$$

the Planck relation becomes the following

$$E = \frac{hc}{\lambda}$$

$$c = 3.000 \times 10^8 \text{ m/s}$$

$$h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s (or J/Hz)}$$

DIRECTIONS: Answer the following in the space provided.

6. What is the wavelength of a wave having a frequency of $3.76 \times 10^{14} \text{ s}^{-1}$?

$$\lambda = ?$$

$$\nu = 3.76 \times 10^{14} \text{ s}^{-1} \text{ (s}^{-1} = /\text{s)}$$

$$\nu = \frac{c}{\lambda} \Rightarrow \lambda = \frac{c}{\nu} \Rightarrow \lambda = \frac{3.000 \times 10^8 \text{ m/s}}{3.76 \times 10^{14} / \text{s}} = \boxed{7.9787 \times 10^{-7} \text{ m}}$$

7. What is the frequency of a $6.9 \times 10^{-13} \text{ m}$ wave?

$$\nu = ?$$

$$\lambda = 6.9 \times 10^{-13} \text{ m}$$

$$\nu = \frac{c}{\lambda} \Rightarrow \nu = \frac{3.000 \times 10^8 \text{ m/s}}{6.9 \times 10^{-13} \text{ m}} = \boxed{4.3478 \times 10^{20} \text{ Hz}}$$

8. What is the wavelength of a 2.990 MHz wave?

$$\lambda = ?$$

$$\nu = 2.990 \text{ MHz} \Rightarrow 2.990 \times 10^6 \text{ Hz (Hz = /s)}$$

$$\nu = \frac{c}{\lambda} \Rightarrow \lambda = \frac{c}{\nu} \Rightarrow \lambda = \frac{3.000 \times 10^8 \text{ m/s}}{2.990 \times 10^6 / \text{s}} = \boxed{100.334 \text{ m}}$$

9. What is the wavelength of a $1.28 \times 10^{17} \text{ Hz}$ wave?

$$\lambda = ?$$

$$\nu = 1.28 \times 10^{17} \text{ Hz (Hz = /s)}$$

$$\nu = \frac{c}{\lambda} \Rightarrow \lambda = \frac{c}{\nu} \Rightarrow \lambda = \frac{3.000 \times 10^8 \text{ m/s}}{1.28 \times 10^{17} / \text{s}} = \boxed{2.3437 \times 10^{-9} \text{ m}}$$

10. What is the frequency of a 2600 cm wave?

$$\nu = ?$$

$$\lambda = 2600 \text{ cm} \Rightarrow 26 \text{ m}$$

$$\nu = \frac{c}{\lambda} \Rightarrow \nu = \frac{3.000 \times 10^8 \text{ m/s}}{26 \text{ m}} = \boxed{1.1538 \times 10^7 \text{ Hz}}$$

11. What is the wavelength of 109.60 MHz wave?

$$\lambda = ?$$

$$\nu = 109.60 \text{ MHz} \Rightarrow 1.0960 \times 10^8 \text{ Hz (Hz = /s)}$$

$$\nu = \frac{c}{\lambda} \Rightarrow \lambda = \frac{c}{\nu} \Rightarrow \lambda = \frac{3.000 \times 10^8 \text{ m/s}}{1.0960 \times 10^8 / \text{s}} = \boxed{2.7372 \text{ m}}$$

12. What is the energy of a $7.66 \times 10^{14} \text{ Hz}$ wave?

$$E = ?$$

$$\nu = 7.66 \times 10^{14} \text{ Hz (Hz = /s)}$$

$$E = h\nu$$

$$E = (6.6262 \times 10^{-34} \text{ J}\cdot\text{s})(7.66 \times 10^{14} / \text{s}) = \boxed{5.0756 \times 10^{-19} \text{ J}}$$

13. What is the frequency of a wave carrying $8.35 \times 10^{-18} \text{ J}$ of energy?

$$\nu = ?$$

$$E = 8.35 \times 10^{-18} \text{ J}$$

$$E = h\nu \Rightarrow \nu = \frac{E}{h} \Rightarrow \nu = \frac{8.35 \times 10^{-18} \text{ J}}{6.6262 \times 10^{-34} \text{ J}\cdot\text{s}} = \boxed{1.2601 \times 10^{16} \text{ Hz}}$$

14. What is the energy of a $3.12 \times 10^{18} \text{ s}^{-1}$ wave?

$$E = ?$$

$$\nu = 3.12 \times 10^{18} \text{ s}^{-1} \text{ (s}^{-1} = /\text{s)}$$

$$E = h\nu$$

$$E = (6.6262 \times 10^{-34} \text{ J}\cdot\text{s})(3.12 \times 10^{18} / \text{s}) = \boxed{2.0673 \times 10^{-15} \text{ J}}$$

15. What is the frequency of a $1.310 \times 10^{-22} \text{ J}$ wave?

$$\nu = ?$$

$$E = 1.310 \times 10^{-22} \text{ J}$$

$$E = h\nu \Rightarrow \nu = \frac{E}{h} \Rightarrow \nu = \frac{1.310 \times 10^{-22} \text{ J}}{6.6262 \times 10^{-34} \text{ J}\cdot\text{s}} = \boxed{1.9770 \times 10^{11} \text{ Hz}}$$

16. What is the energy of a 9330 cm wave?

$$E = ?$$

$$\lambda = 9330 \text{ cm} \Rightarrow 93.3 \text{ m}$$

$$E = \frac{hc}{\lambda} \Rightarrow E = \frac{(6.6262 \times 10^{-34} \text{ J}\cdot\text{s})(3.000 \times 10^8 \text{ m/s})}{93.3 \text{ m}} = \boxed{2.1306 \times 10^{-27} \text{ J}}$$

17. What is the wavelength of a $1.528 \times 10^{-13} \text{ J}$ wave?

$$\lambda = ?$$

$$E = 1.528 \times 10^{-13} \text{ J}$$

$$E = \frac{hc}{\lambda} \Rightarrow \lambda = \frac{hc}{E}$$

$$\lambda = \frac{(6.6262 \times 10^{-34} \text{ J}\cdot\text{s})(3.000 \times 10^8 \text{ m/s})}{1.528 \times 10^{-13} \text{ J}} = \boxed{1.300955 \times 10^{-12} \text{ m}}$$